

- Base Groups
- Uniform circular motion
- Forces

PHYS 210 General Physics I

$F_{\text{Drag}} \propto v$

Base Groups

- ▶ BGDG: What's one of the strangest things you've ever seen?
- ▶ BGWS
- ▶ RQ



Uniform Circular Motion

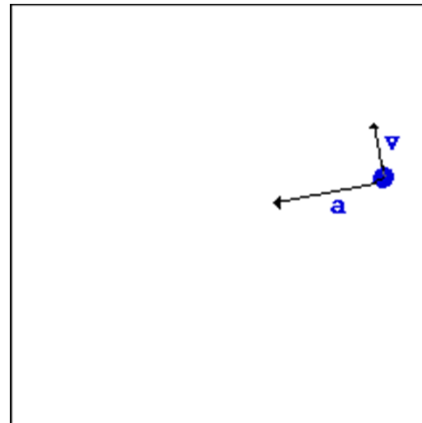
- ▶ Uniform = constant speed
- ▶ Circular = non-constant acceleration!
- ▶ The centripetal acceleration is
 - $a_c = v^2/r$, where r = radius of circular path
 - a_c is constant in magnitude, not direction
 - At any instant in time, the (constant speed) velocity vector is ...
tangent to the circular path!

Uniform circular motion

- ▶ Note that the acceleration vector is not constant!
- ▶ But the magnitude of $\vec{a}$ is constant:

$$|\vec{a}| = \frac{v^2}{r}$$

where r = radius of circular path



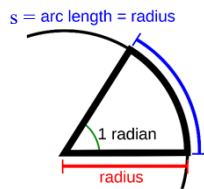
Rotational Motion – the variables

Rotational motion has variables that are closely analogous to those of linear motion

$$s = r\theta = \text{arclength}$$

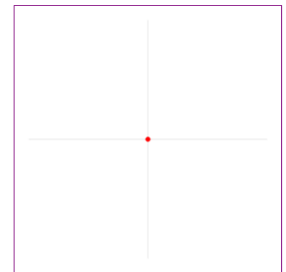
Rotational Motion – the variables

Unit of angular measure: degrees or radians



$$\theta = \frac{s}{r}$$

$$\begin{aligned} 2\pi \text{ rad} &= 360^\circ \\ \pi \text{ rad} &= 180^\circ \end{aligned}$$



- An angle in radians is the ratio of two lengths, so has no “units”
- It's the number of radii along an arclength
- We often indicate angles in radians with the “unit” of *rad*

Rotational Motion – the variables

Rotational motion has variables that are closely analogous to those of linear motion

$$s = r\theta = \text{arclength}$$

Angular velocity

$$\omega = \frac{d\theta}{dt}$$

Direction?

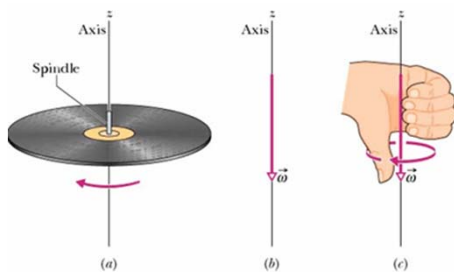
Use a RH rule!

Angular acceleration

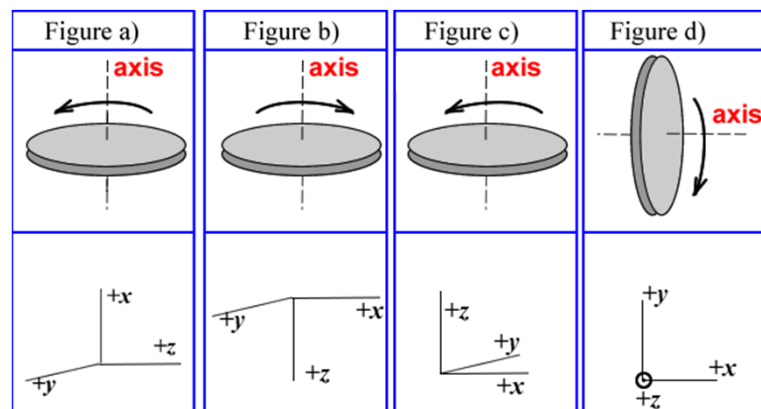
$$\vec{\alpha} = \frac{d\vec{\omega}}{dt}$$

Direction – check out ω

Rotational Motion – the variables



RHR for direction of $\vec{\omega}$



Direction of $\vec{\omega}$ and $\vec{\alpha}$ if $|\vec{\omega}|$ is increasing?

Direction of $\vec{\omega}$ and $\vec{\alpha}$ if $|\vec{\omega}|$ is decreasing?

Constant angular acceleration



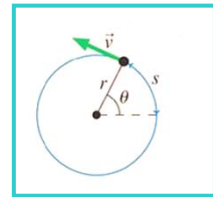
MISSING
QUANTITY

Equations for const.
angular acceleration

$$\begin{aligned}\omega &= \omega_o + \alpha \Delta t \\ \theta &= \theta_o + \omega_o \Delta t + \frac{1}{2} \alpha \Delta t^2 \\ \omega^2 &= \omega_o^2 + 2\alpha(\theta - \theta_o) \\ \theta &= \theta_o + \frac{1}{2}(\omega + \omega_o)\Delta t \\ \theta &= \theta_o + \omega \Delta t - \frac{1}{2} \alpha \Delta t^2\end{aligned}$$

θ, θ_o
 ω
 Δt
 α
 ω_o

$$\begin{aligned}\omega_f &= \omega_i + \alpha \Delta t \\ \theta_f &= \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha \Delta t^2 \\ \omega_f^2 &= \omega_i^2 + 2\alpha(\theta_f - \theta_i)\end{aligned}$$



Constant angular acceleration

Rotational kinematics

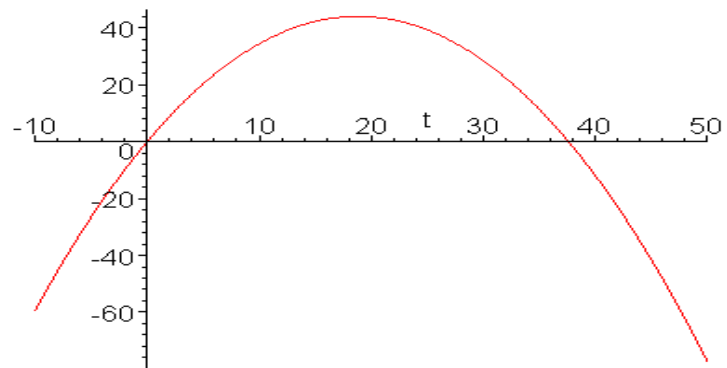
Linear kinematics

$$\begin{aligned}\omega_f &= \omega_i + \alpha \Delta t \\ \theta_f &= \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2 \\ \omega_f^2 &= \omega_i^2 + 2\alpha \Delta \theta\end{aligned}$$

$$\begin{aligned}v_{fs} &= v_{is} + a_s \Delta t \\ s_f &= s_i + v_{is} \Delta t + \frac{1}{2} a_s (\Delta t)^2 \\ v_{fs}^2 &= v_{is}^2 + 2a_s \Delta s\end{aligned}$$



EX: At $t = 0$, a flywheel has an angular velocity of 4.7 rad/s , a constant angular acceleration of -0.25 rad/s^2 , and a reference line at $\theta_0 = 0$. (a) Through what max angle will the reference line turn in the positive direction? What are the (b) first and (c) second times the ref line will be at $\theta = \theta_{\text{max}}$?



PHYS 210 - General Physics I

FORCES



- Rotational kinematics
- Forces!



**Have a reasonably good
Wednesday!**